

# The Gallery of Infinite Series

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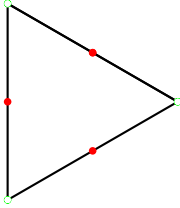
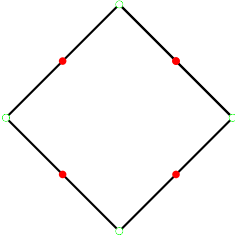
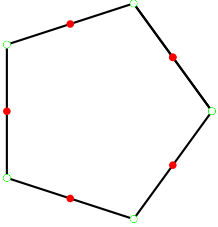
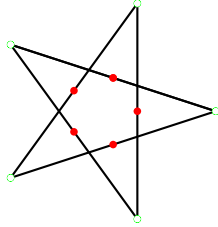
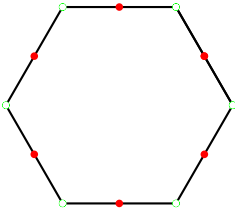
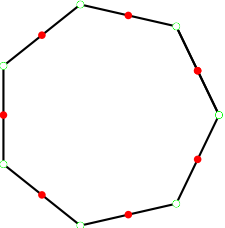
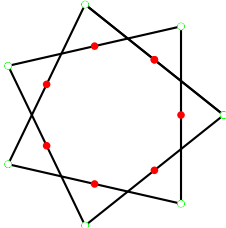
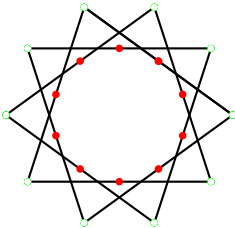
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# 1 Real polygons

There are the polytopes  $2\{\frac{p}{q}\}_2$  (with  $p$  and  $q$  in  $\mathbb{N}$ ) in the notation of Coxeter. Use the command:

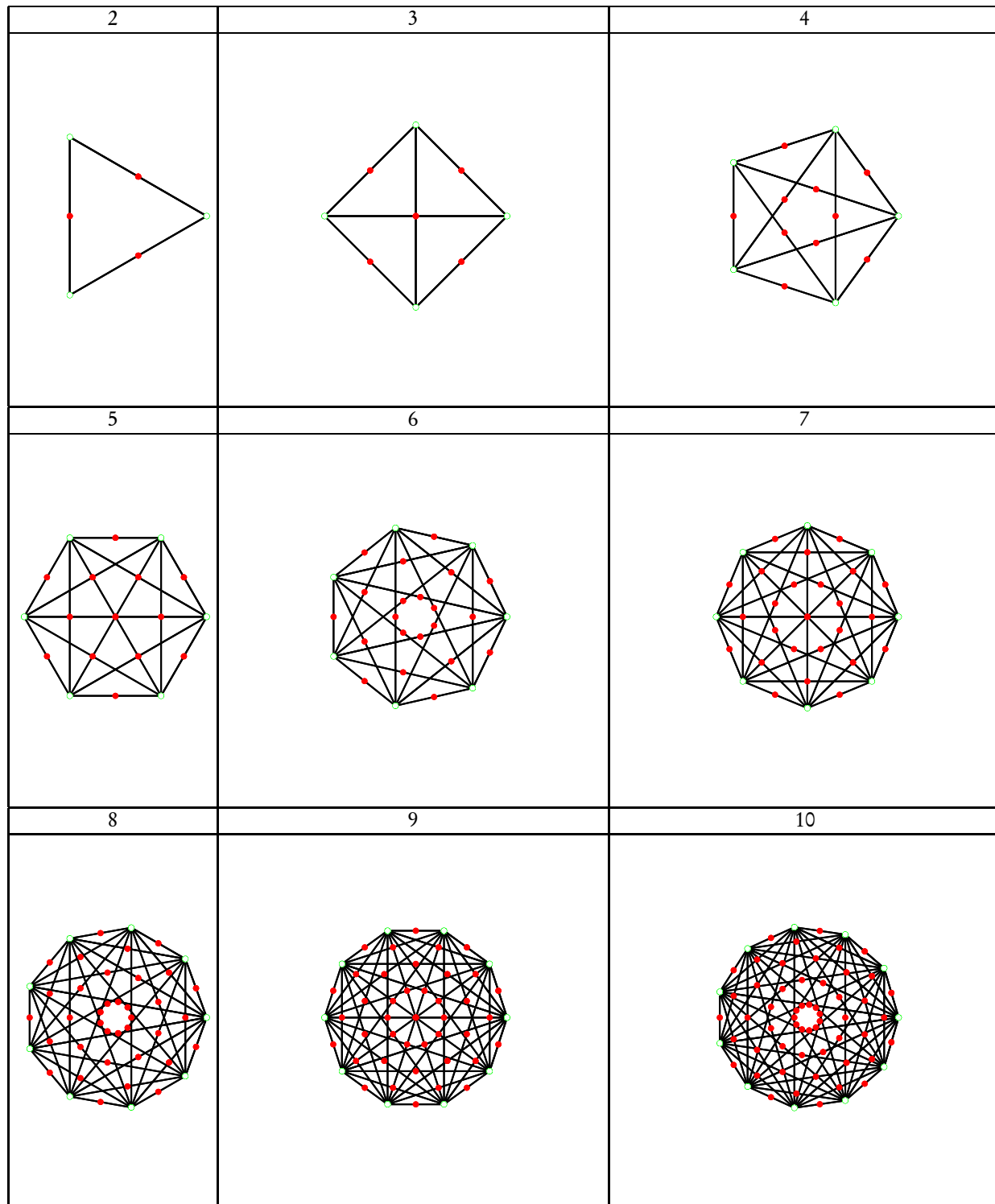
`\psset{unit=1.5cm}\Polygon[P=p,Q=q]`

2	3	4
		
5	$\frac{5}{2}$	6
		
7	$\frac{7}{2}$	$\frac{7}{3}$
		

## 2 Simplices

There are the real polytopes  $2\{3\}2 \cdots 2\{3\}2$  in dimension  $n$  (tetrahedron, pentatope, sextatope etc...) in the notation of Coxeter. Use the command:

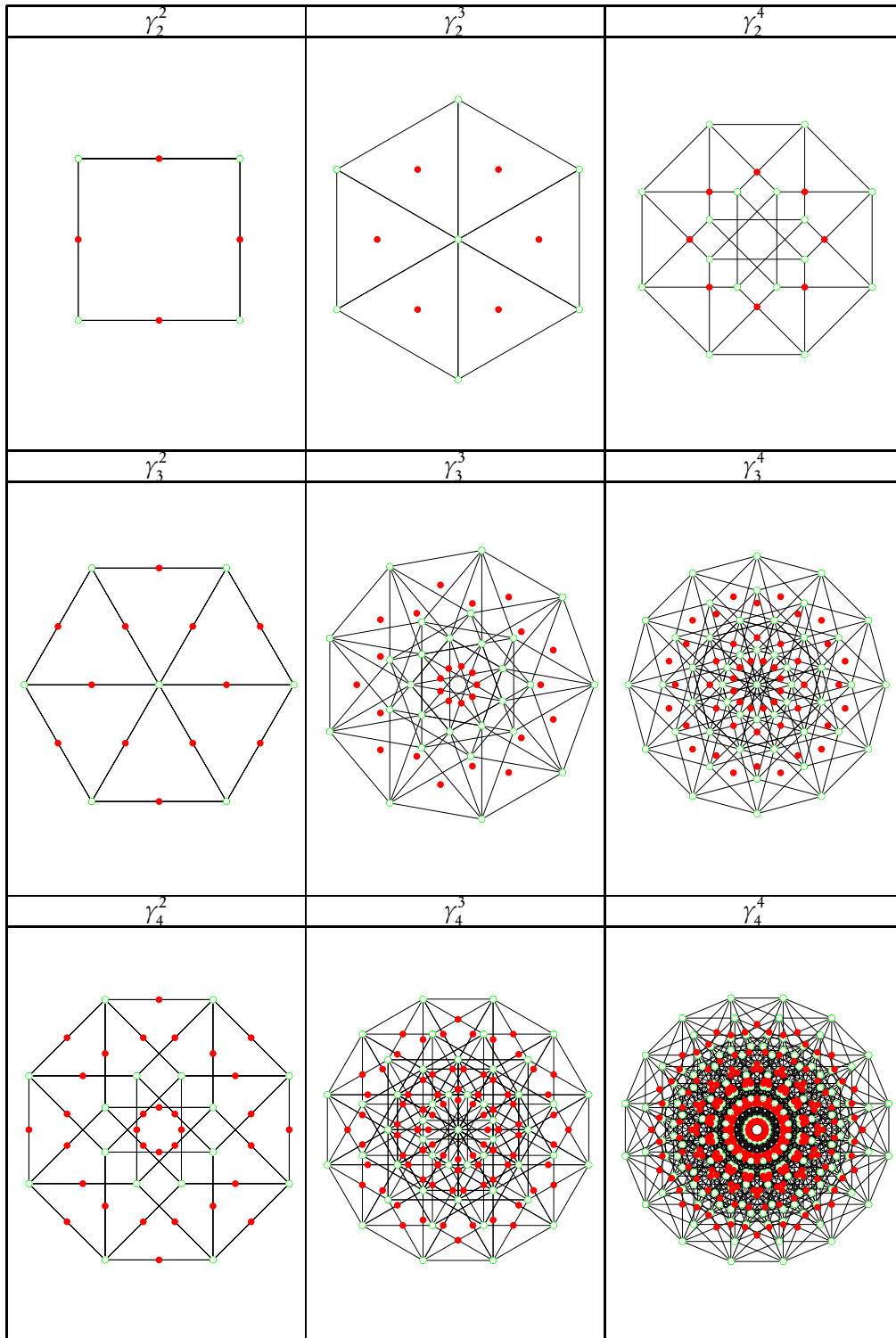
`\psset{unit=1.5cm}\Simplex[dimension=n]`



### 3 The infinite series $\gamma_n^p$

It is an infinite series of polytopes with two parameters  $p$  and  $n$ . The parameter  $n$  is the dimension of the polytope. In the notation of Coxeter, its name reads  $p\{4\}2\{3\}\dots\{3\}2$ . In the case  $p = 2$ , we recover the family of the hypercubes. Use the command:

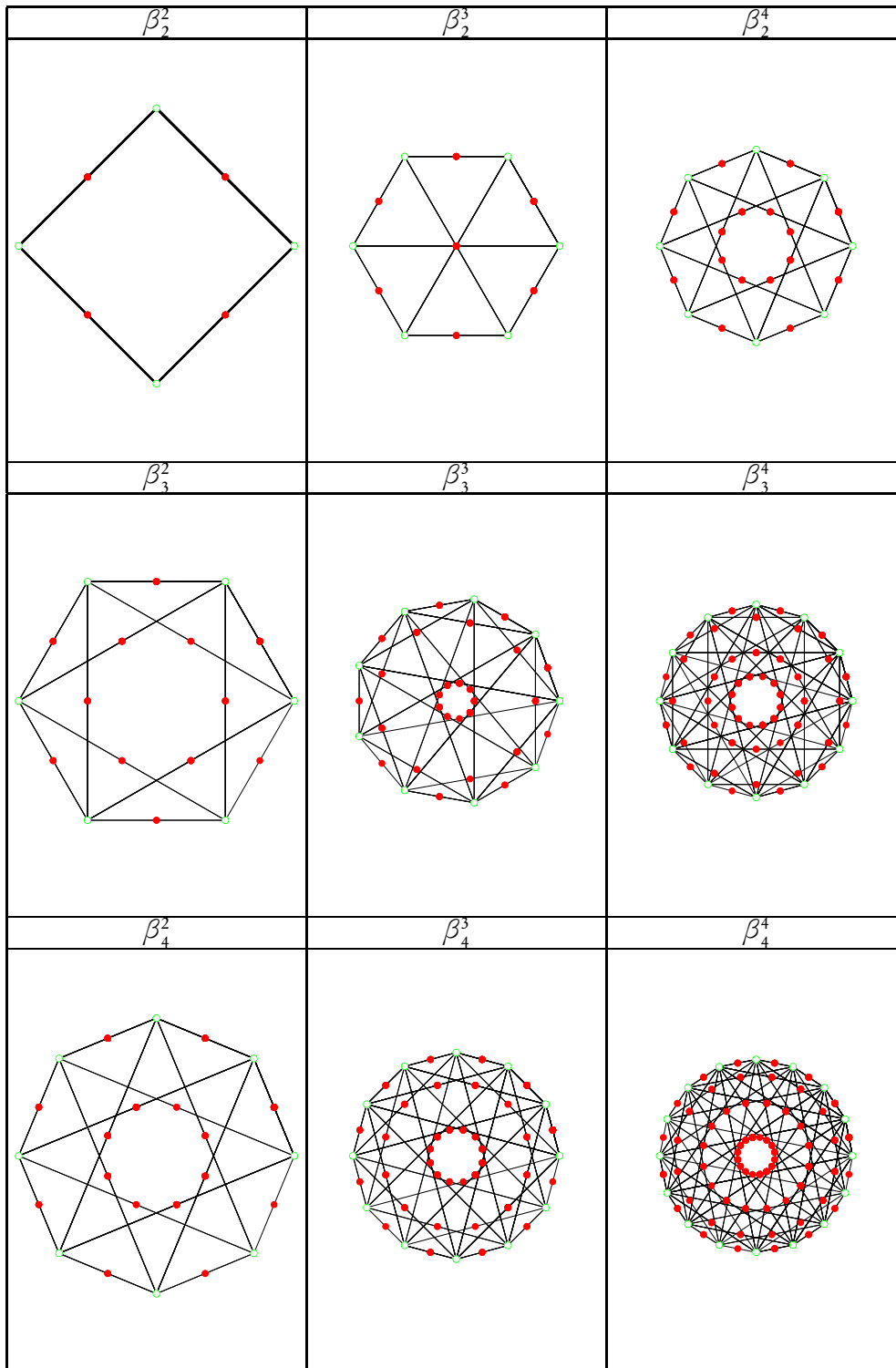
`\gammavn[P=p,dimension=n]`



## 4 The infinite series $\beta_n^p$

It is an infinite series of polytopes with two parameters  $p$  and  $n$  reciprocals of  $\gamma_n^p$ . The parameter  $n$  is the dimension of the polytope. In the notation of Coxeter, its name reads  $2\{3\}2\{3\}\dots\{3\}2\{4\}p$ . In the case  $p = 2$ , we recover the family of the  $2^n$ -topes which generalizes the tetrahedron for higher dimension. Use the command:

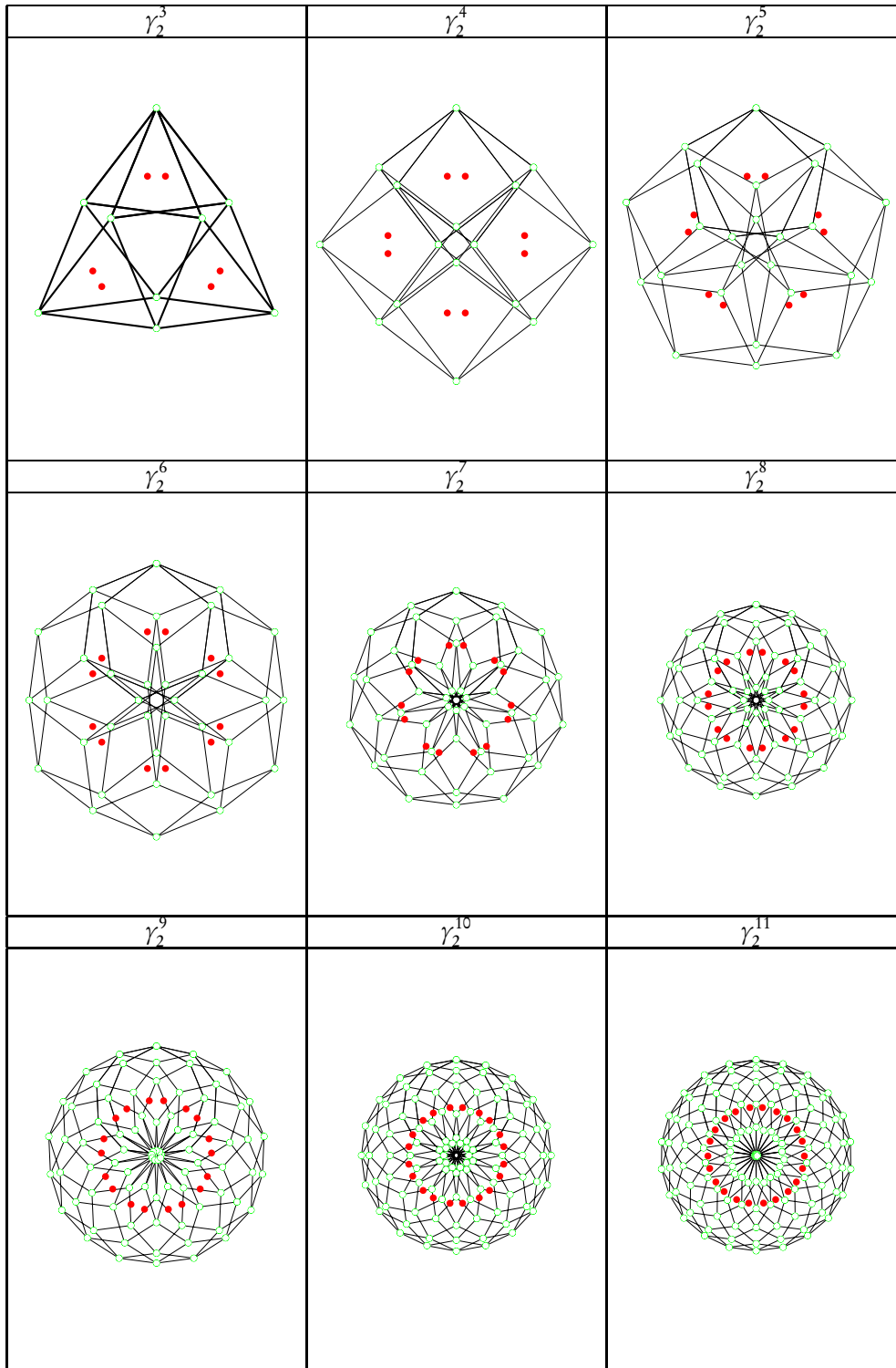
`\betapn[P=p,dimension=n]`



## 5 The infinite series $\gamma_2^p$

It is a special case of the series  $\gamma_n^p$  for  $n = 2$ . In this case, the polytopes are complex polygons. The projection used here is different than the projection used with `gammamn`. Use the command:

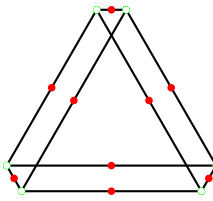
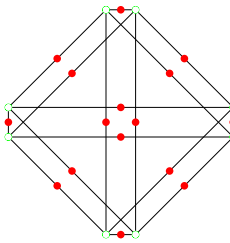
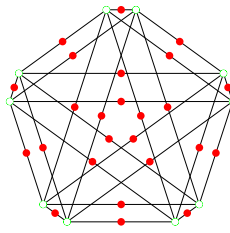
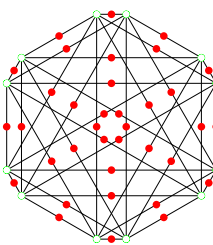
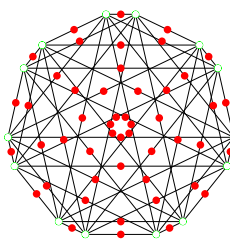
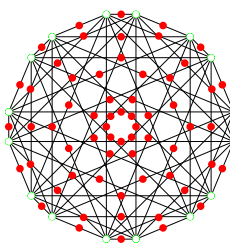
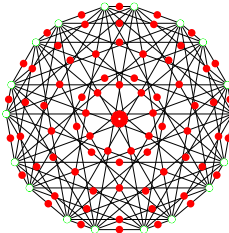
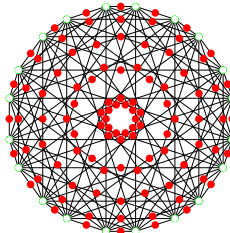
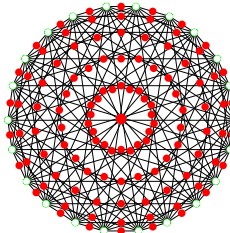
`\gammaptwo[P=p]`



## 6 The infinite series $\beta_2^p$

It is a special case of the series  $\beta_n^p$  for  $n = 2$ . In this case, the polytopes are complex polygons. The projection used here is different than the projection used with `betapn`. Use the command:

`\betaptwo[P=p]`

$\beta_2^3$	$\beta_2^4$	$\beta_2^5$
		
$\beta_2^6$	$\beta_2^7$	$\beta_2^8$
		
$\beta_2^9$	$\beta_2^{10}$	$\beta_2^{11}$
		

## References

- [1] H. S. M. Coxeter, *Regular Complex Polytopes*, Second Edition, Cambridge University Press, 1991 .